### **Black Swans, Dragons-Kings and Prediction**

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www.er.ethz.ch





#### **EXTREME EVENTS in Natural SYSTEMS**

- •Earthquakes
- •Volcanic eruptions
- •Hurricanes and tornadoes
- •Landslides, mountain collapses
- •Avalanches, glacier collapses
- •Lightning strikes
- •Meteorites, asteroid impacts
- •Catastrophic events of environmental degradations



#### **EXTREME EVENTS in SOCIO-ECONOMIC SYSTEMS**

- •Failure of engineering structures
- •Crashes in the stock markets
- •Social unrests leading to large scale strikes and upheavals
- •Economic recessions on regional and global scales
- •Power blackouts
- •Traffic gridlocks
- •Social epidemics
- •Block-busters
- •Discoveries-innovations
- •Social groups, cities, firms...
- •Nations
- •Religions...



# **Extreme events are epoch changing** in the physical structure and in the mental spaces

- Droughts and the collapse of the Mayas (760-930 CE)... and many others...
- French revolution (1789) and the formation of Nation states
- Great depression and Glass-Steagall act
- Crash of 19 Oct. 1987 and volatility smile (crash risk)
- Enron and Worldcom accounting scandals and Sarbanes-Oxley (2002)
- Great Recession 2007-2009: consequences to be seen...



#### **2008 FINANCIAL CRISIS**





Jean-Pierre Danthine: Swiss monetary policy and Target2-Securities Introductory remarks by Mr Jean-Pierre Danthine, Member of the Governing Board of the Swiss National Bank, at the end-of-year media news conference, Zurich, 16 December 2010.



#### Federal Reserve balance sheet



# Black Swan story

#### Unknown unknowable event

- cannot be diagnosed in advance, cannot be quantified, no predictability
- No responsability ("wrath of God")
- One unique strategy: long put options and insurance

#### Chart 1: HOME PRICES - STILL DEFLATING AFTER ALL THESE YEARS

#### United States

S&P/Case-Shiller Home Price Index: Composite 20 (Jan 2000 = 100, seasonally adjusted)





Source: IMF Global Financial Stability Report; World Economic Outlook November update and estimates; World Federation of Exchanges.

# **Self-organized criticality**



(Bak, Tang, Wiesenfeld, 1987)





#### **Earthquakes Cannot Be Predicted**

Robert J. Geller, David D. Jackson, Yan Y. Kagan, Francesco Mulargia Science 275, 1616-1617 (1997)



#### Heavy tails in pdf of earthquakes

#### Heavy tails in pdf of seismic rates





#### Heavy tails in pdf of rock falls, Landslides, mountain collapses



Turcotte (1999)

#### Heavy tails in pdf of forest fires



**Fig. 2.** Noncumulative frequency-area distributions for actual forest fires and wildfires in the United States and Australia: (**A**) 4284 fires on U.S. Fish and Wildlife Service lands (1986–1995) (9), (**B**) 120 fires in the westem United States (1150–1960) (10), (**C**) 164 fires in Alaskan boreal forests (1990–1991) (11), and (**D**) 298 fires in the ACT (1926–1991) (12). For each data set, the noncumulative number of fires per year  $(-d\dot{N}_{cF}/dA_{F})$  with area ( $A_{F}$ ) is given as a function of  $A_{F}$  (13). In each case, a reasonably good correlation over many decades of  $A_{F}$  is obtained by using the power-law relation (Eq. 1) with  $\alpha = 1.31$  to 1.49,  $-\alpha$  is the slope of the best-fit line in log-log space and is shown for each data set.

Malamud et al., Science 281 (1998)



#### Heavy tails in pdf of Hurricane losses





13



x<sub>min</sub>=7

Severity of event, x - Number of people killed (or injured)

0.0001









Real Corporate Profits

#### Most crises are "endogenous"

can be diagnosed in advance,
 can be quantified, (some) predictability

- Moral hazard, conflict of interest, role of regulations
- Responsibility, accountability
- Strategic vs tactical timedependent strategy
- Weak versus global signals



http://www.businessweek.com/the\_thread/economicsunbound/archives/2009/03/a\_bad\_decade\_fo.html 3

### Beyond power laws: 7 examples of "Dragons"

Financial economics: Outliers and dragons in the distribution of financial drawdowns.

**Population geography**: Paris as the dragon-king in the Zipf distribution of French city sizes.

Material science: failure and rupture processes.

Hydrodynamics: Extreme dragon events in the pdf of turbulent velocity fluctuations.

Metastable states in random media: Self-organized critical random directed polymers Brain medicine: Epileptic seizures

**Geophysics**: Characteristic earthquakes? Great avalanches? Floods? Mountain collapses? Meteological events? and so on



#### **Better risk measure: drawdowns**





### "Dragons" of financial risks

(require special mechanism and may be more predictable)





-bubble phase -crash phase

$$\frac{dp}{dt} = cp^d$$

$$p(t) = \left(\frac{c}{m}\right)^{-m} (t_c - t)^{-m}$$

$$m = 1/(d-1) > 0$$
 and  $t_c = t_0 + mp_0^{1-d}/c$ .

Bubble preparing a crisis: **Faster than exponential** transient unsustainable growth of price **Finite-time Singularity** 

#### as a result of positive feedbacks



• Planet formation in solar system by run-away accretion of planetesimals

• PDE's: Euler equations of inviscid fluids and relationship with turbulence

• PDE's of General Relativity coupled to a mass field leading to the formation of black holes

• Zakharov-equation of beam-driven Langmuir turbulence in plasma

- $\bullet$  rupture and material failure
- Earthquakes (ex: slip-velocity Ruina-Dieterich friction law and accelerating creep)
- Models of micro-organisms chemotaxis, aggregating to form fruiting bodies
- Surface instability spikes (Mullins-Sekerka), jets from a singular surface, fluid drop snap-off
- Euler's disk (rotating coin)
- Stock market crashes...

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25

Metastable states in random media: Self-organized critical random directed polymers Brain medicine: Epileptic seizures Geophysics: Gutenberg-Richter law and characteristic

earthquakes.



Fig. 7. French agglomerations: stretched exponential and "King effect".

Jean Laherrere and Didier Sornette, Stretched exponential distributions in Nature and Economy: ``Fat tails'' with characteristic scales, European Physical Journal B 2, 525-539 (1998)

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Energy distribution for the [+-62] specimen #4 at different times, for 5 time windows with 3400 events each. The average time (in seconds) of events in each window is given in the caption.

#### time-to-failure analysis

S.G. Sammis and D. Sornette, Positive Feedback, Memory and the Predictability of Earthquakes, Proceedings of the National Academy of Sciences USA, V99 SUPP1:2501-2508 (2002 FEB 19)

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Mathematical Geophysics Conference Extreme Earth Events Villefranche-sur-Mer, 18-23 June 2000



L'vov, V.S., Pomyalov, A. and Procaccia, I. (2001) Outliers, Extreme Events and Multiscaling, Physical Review E 6305 (5), 6118, U158-U166.

FIG. 3.2. Apparent probability distribution function of the square of the fluid velocity, normalized to its time average, in the eleventh shell of the toy model of hydrodynamic turbulence discussed in the text. The vertical axis is in logarithmic scale such that the straight line, which helps the eye, qualifies as an apparent exponential distribution. Note the appearance of extremely sparse and large bursts of velocities at the extreme right above the extrapolation of the straight line. Reproduced from [252].



Pdf of the square of the Velocity as in the previous figure but for a much longer time series, so that the tail of the distributions for large Fluctuations is much better constrained. The hypothesis that there are no outliers is tested here by collapsing the distributions for the three shown layers. While this is a success for small fluctuations, the tails of the distributions for large events are very different, indicating that extreme fluctuations belong to a different class of their own and hence are outliers.

L'vov, V.S., Pomyalov, A. and Procaccia, I. (2001) Outliers, Extreme Events and Multiscaling, Physical Review E 6305 (5), 6118, U158-U166.

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#### Metastable states in random media Self-organized critical random directed polymers



FIG. 1. Typical set of optimal configurations for a RDP of length W = 4096 and for  $0 \le y \le 1200$ : (a) global system [gray framed boxes outline regions of succeeding plots such that the horizontal and vertical extensions of these boxes follow Eqs. (10) and (8) with  $\alpha \approx 0.9$ ], (b) magnification of the largest box in (a), (c) magnification of the largest box in (b) and (d) magnification of the box in (c). Note, that at each grid point of the lattice we assign an independent random number drawn from an exponential distribution with unit mean and variance.

# Definition of "avalanches" Y L y+1 y Χ W 0

FIG. 2. Schematic representation of optimal RDPs fixed at their two end points. An avalanche is defined by the area *S* spanned by the transition from the optimal configuration at *y* to y+1, i.e., *S* is the area interior to the perimeter formed by the union of the two optimal RDP configurations at *y* and y+1 and the two vertical segments ((0,y);(0,y+1)) and ((W,y);(W,y+1)). The successive avalanches are represented in different gray scales.



FIG. 4. P(S) as a function of the rescaled variable  $S/W^{5/3}$  for W = 8 - 512 on a log-log plot.

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#### 1. Geosciences of the solid envelop

- 1.1. Earthquake magnitude.
- 1.2. Volcanic eruptions.
- 1.3. Landslides.
- 1.4. Floods. No protagonist found yet.

#### 2. Meteorological and Climate sciences

- 2.1. Rains, hurricanes, storms.
- 2.2. Snow avalanches.

#### 3. Material Sciences and Mechanical Engineering

- 3.1. Acoustic emissions.
- 3.2. Hydrodynamic turbulence.
- 4. Economics : financial drawdowns, distribution of wealth
- 5. Social sciences: distribution of firm sizes, of city sizes, of social groups...
- 6. Social sciences : wars, strikes, revolutions, city sizes
- 7. Medicine: epileptic seizures, epidemics

8. Environmental sciences : extinctions of species, forest fires
8.1. Evolution and extinction of species.
8.2. Forest fires.

Special Issue SPRINGER G. Ouillon and D. Sornette Guest Editors (2011)

### **Mechanisms for Dragon-kings**

Generalized correlated percolation

•A kind of condensation (a la Bose-Einstein)

Partial global synchronization

#### Dynamic clustering in N balls in a billiard

Two balls are D-*neighbors* at epoch t if they collided during the time interval [t-D, t]. Any connected component of this neighbor relation is called a D-cluster at epoch t.



#### Landau-Ginzburg Theory of Self-Organized Criticality and of Dragon-kings!

Dynamics of an order parameter (OP) and of the corresponding *control* parameter (CP): within the sandpile picture,  $\frac{\partial h}{\partial x}$  is the slope of the sandpile, h being the local height, and S is the state variable distinguishing between static grains (S = 0) and rolling grains ( $S \neq 0$ ).

L. Gil and D. Sornette "Landau-Ginzburg theory of selforganized criticality", Phys. Rev.Lett. 76, 3991-3994 (1996)

#### Normal form of sub-critical bifurcation

$$\frac{\partial S}{\partial t} = \chi \left\{ \mu S + 2\beta S^3 - S^5 \right\} \tag{1}$$

where

$$\mu = \left[ \left( \frac{\partial h}{\partial x} \right)^2 - \left( \frac{\partial h}{\partial x} |_c \right)^2 \right]$$

and  $\beta > 0$  (subcritical condition).

Diffusion equation

$$\frac{\partial h}{\partial t} = -\frac{\partial F\left(S, \frac{\partial h}{\partial x}\right)}{\partial x} + \Phi$$

$$(2)$$

(3)

$$F\left(S,\frac{\partial h}{\partial x}\right) = -\alpha \frac{\partial h}{\partial x}S^2, \qquad \alpha > 0$$





FIG. 3. Distribution P(J) of flux amplitudes at the right border, in the same conditions as for Fig. 1.

#### **Global auroral energy deposition**

Auroral Blob Analysis from Polar UVI (Jan 1-31, 1997)





10% daily drop on Nasdaq : 1/1000 probability

1 in 1000 days  $\implies$  1 day in 4 years

30% drop in three consecutive days?

 $(1/1000)^{*}(1/1000)^{*}(1/1000) = (1/1000,000,000)$ 

=> one event in 4 millions years!



### Mechanisms for positive feedbacks in the stock market

### • Technical and rational mechanisms

- 1. Option hedging
- 2. Insurance portfolio strategies
- 3. Trend following investment strategies
- 4. Asymmetric information on hedging strategies

### • Behavioral mechanisms:

- 1. Breakdown of "psychological Galilean invariance"
- 2. Imitation(many persons)
  - a) It is rational to imitate
  - b) It is the highest cognitive task to imitate
  - c) We mostly learn by imitation
  - d) The concept of "CONVENTION" (Orléan)
- 3. "Social Proof" mechanism





#### **Financial Instability Hypothesis (Minsky)**



# Predictability of the 2007-XXXX crisis: 15y History of bubbles and Dragon-kings

- The ITC "new economy" bubble (1995-2000)
- Slaving of the Fed monetary policy to the stock market descent (2000-2003)
- Real-estate bubbles (2003-2006)
- MBS, CDOs bubble (2004-2007)
- Stock market bubble (2004-2007)
- Commodities and Oil bubbles (2006-2008)

Didier Sornette and Ryan Woodard Financial Bubbles, Real Estate bubbles, Derivative Bubbles, and the Financial and Economic Crisis (2009) (<u>http://arxiv.org/abs/0905.0220</u>)

#### The illusionary "PERPETUAL MONEY MACHINE"



120



Rate of profit and rate of accumulation: The United States + European Union + Japan

\* Rate of accumulation = rate of growth rate of the net volume of capital \* Rate of profit = profit/ capital (base: 100 in 2000)

Sources and data of the graphs: <a href="http://hussonet.free.fr/toxicap.xls">http://hussonet.free.fr/toxicap.xls</a>

Thee gap widens between the share of wages and the share of consumption (gray zones), so as to compensate for the difference between profit and accumulation. FINANCE allows increasing debt and virtual wealth growh... which can only be transitory (even if very long).

# United States Share of wages and of private consumption in Gross Domestic Product (GDP)

Source of data and graphics: <u>http://</u> <u>hussonet.free.fr/toxicap.xls</u>

### **Wealth Extraction**

Over the past decade and a half, (B - F) has been closely correlated with realized capital gains on the sale of homes. B-F=change in home equity debt outstanding less unscheduled repayment on RMDO

Mortgage Equity Withdrawal impact on GDP



#### **THE NASDAQ CRASH OF APRIL 2000**







### **The Global BUBBLE**



PCA first component on a data set containing, emerging markets equity indices, freight indices, soft commodities, base and precious metals, energy, currencies...

(Peter Cauwels FORTIS BANK - Global Markets)

# New risks to consider

- Inflation and Deflation
- Bank failures
- "Government risks"
- Economic Slowdown (China)

•Financial instabilities are developing everywhere and will develop even more than in the past.

•Systemic risks are rising planet-wise, with entangling of many risk components (everything is linked).

# **Towards new asset allocation strategies**

### **1- Fundamental allocation**

-strategic allocation in energy, environment, commodities...

### **2-** Tactical allocation

-Bubble diagnostic (targeted, scanning, global...)

-Global and local crash alarm indices

-Improved timing (TaR: Time @ Risk)

ETH

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# FCO@ETH: Towards operational science of financial instabilities

- Main mission:
  - Identify bubbles
- Theory:
  - Positive feedback
- Deliverables
  - Weekly global bubble scan
  - Research, papers
  - Public forecasts
  - Digital timestamps

Didier Sornette, Maxim Fedorovsky, Stefan Riemann, Hilary Woodard, Ryan Woodard, Wanfeng Yan, Wei-Xing Zhou







### **The Financial Bubble Experiment** First Results (2 November 2009 - 3 May 2010)

D. Sornette, R. Woodard, M. Fedorovsky, S. Reimann, H. Woodard, W.-X. Zhou (The Financial Crisis Observatory) Department of Management, Technology and Economics, ETH Zurich, Kreuzplatz 5, CH-8032 Zurich, Switzerland



### **Methodology for predictability of crises**

Strategy: look at the forest rather than at the tree



Our prediction system is now used in the industrial phase as the standard testing procedure.

EADS



J.-C. Anifrani, C. Le Floc'h, D. Sornette and B. Souillard "Universal Log-periodic correction to renormalization group scaling for rupture stress prediction from acoustic emissions", J.Phys.I France 5, n°6, 631-638 (1995)

### **Methodology for diagnosing bubbles**

# • Inputs:

#### -prices

**-factors** (interest rates, interest spread, historical and implied volatility, exchange rates)

# • Methods:

-Self-consistent calibration of prices (not returns)

-Portolio of methods to identify transient bubble regimes (entropy, hierarchical analysis, reverse engineering with ABM...)





#### Methodology for diagnosing bubbles

# Positive feedbacks of higher return anticipation

\*Super exponential price

\*Power law "Finite-time singularity"

# Negative feedback spirals of crash expectation \*Accelerating large-scale financial volatility \*Log-periodic discrete scale-invariant patterns





# **Generic Prediction Phase Diagram**



### **Black Swans, Dragons-Kings and Prediction**

- An illustration of trans-disciplinarity at work
- Out-of-equilibrium view of the world (social systems, economics, geosciences, biology...)
- Dragon-kings as extreme events are the rule rather than the exception. Their study reveal important new mechanisms.
- Crises are (probabilistically) predictable

### Final remarks

1-All proposals will fail if we do not have better science and better metrics to monitor and diagnose (ex: biology, medicine, astronomy, chemistry, physics, evolution, and so on)

2-Leverage as a system variable versus the illusion of control by monetary policy, risk management, and all that

3-Need to make endogenous policy makers and regulators ("creationist" view of government role, illusion of control and law of unintended consequences of regulations)

4-Fundamental interplay between system instability and growth; the positive side of (some) bubbles

5-Time to reassess goals (growth vs sustainability vs happiness). In the end, endogenous co-evolution of culture, society and economy

KEY CHALLENGE: genuine trans-disciplinarity by **TRAINING in 2-3 disciplines + CHANGE OF CULTURE** 

### **Further Reading**

T. Kaizoji and D. Sornette, Market Bubbles and Crashes, in press in the Encyclopedia of Quantitative Finance (Wiley, 2008) (preprint at <u>http://arxiv.org/abs/0812.2449</u>)

D. Sornette and R. Woodard Financial Bubbles, Real Estate bubbles, Derivative Bubbles, and the Financial and Economic Crisis (preprint at <u>http://arxiv.org/abs/0905.0220</u>) will appear in the Proceedings of APFA7 (Applications of Physics in Financial Analysis, <u>http://www.thic-apfa7.com/en/htm/index.html</u>)

Didier Sornette, Why Stock Markets Crash (Critical Events in Complex Financial Systems) Princeton University Press, January 2003

Y. Malevergne and D. Sornette, Extreme Financial Risks (From Dependence to Risk Management) (Springer, Heidelberg, 2006).